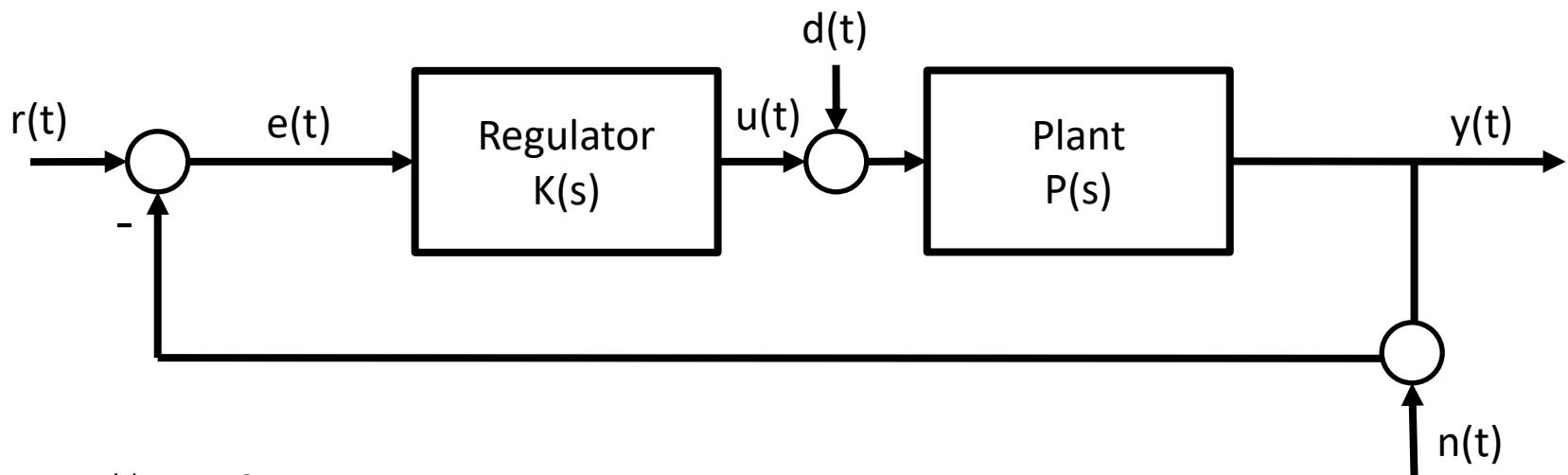


Lecture #0.3

Standard industrial regulators

- Introduction to PID controllers
- PID control law:
 - Ideal
 - Real
- Some rules of thumb

Reference scheme



- $r(t)$ – reference signal
- $e(t)$ – control error
- $u(t)$ – control action
- $y(t)$ – controlled output
- $n(t)$ – measurement noise
- $d(t)$ – additive (control action) disturbance

Standard regulators

- The **dynamic characteristics** of controlled systems can vary greatly depending on the application
- However, it would be convenient to have controllers with a **standard structure**, to be configured according to the application
 - use controllers with a **fixed structure**
 - only tune some **parameters**

Standard regulators

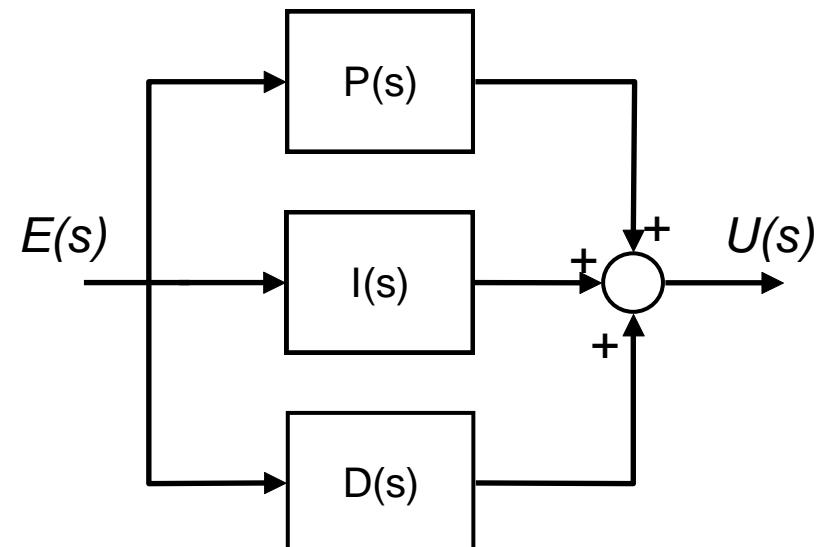
The most common **standard controllers** are

- LTI Controllers
→ Proportional Integral Derivative (PID)
- NL Controllers
→ Relay

Industrial PID regulators

In a **PID regulator** the control action $u(t)$ is obtained as the sum of three terms

1. The first is **proportional** to the error $e(t)$
2. The second is proportional to the **integral** of $e(t)$ (i.e. to its average value);
3. The third is proportional to the **derivative** of $e(t)$



Industrial PID regulators

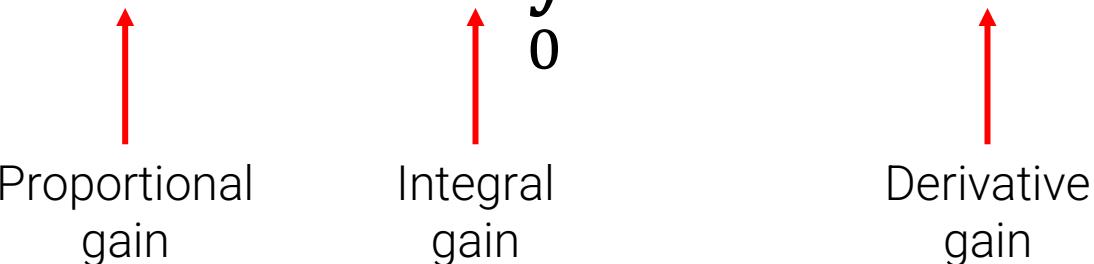
Advantages

The success of PID regulators in the industrial field is essentially due to the following reasons:

- efficiently regulate **processes of different nature** (*thermal, mechanical, etc.*)
- realizable with **different types of technology** (*pneumatic, electronic, etc.*)
- convenience of a **standard structure** (*reduction of project costs, management and maintenance, benefits in the management of warehouse stocks*)
- often **do not require a detailed model** of the process (*auto-tuning procedures also exist*)

Control law

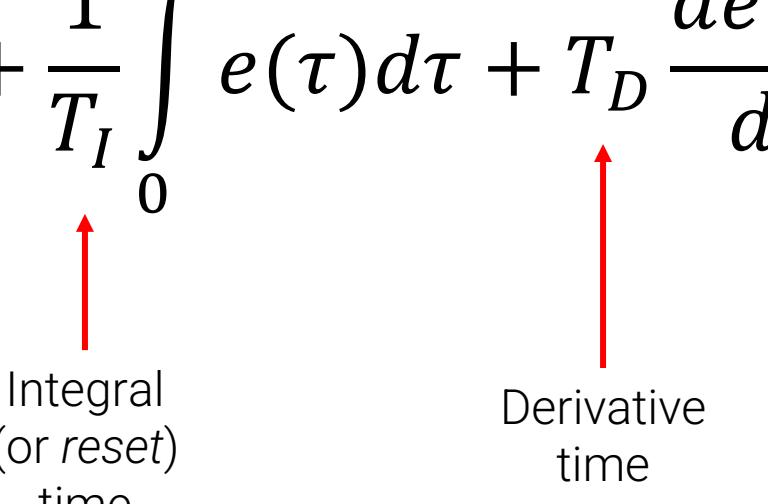
- In the time domain

$$u(t) = K_P e(t) + K_I \int_0^t e(\tau) d\tau + K_D \frac{de(t)}{dt}$$


Proportional gain Integral gain Derivative gain

Control law

- Another common representation:

$$u(t) = K_P \left(e(t) + \frac{1}{T_I} \int_0^t e(\tau) d\tau + T_D \frac{de(t)}{dt} \right)$$


Ideal control law

In the Laplace domain

- **Ideal** control law: it is **not physically achievable (non-proper)**

$$U(s) = K_P \left(1 + \frac{1}{T_I s} + T_D s \right) E(s) = K_P \left(\frac{T_D T_I s^2 + T_I s + 1}{T_I s} \right) E(s)$$

- **Real** control law obtained by **filtering the derivative action**

$$U(s) = K_P \left(1 + \frac{1}{T_I s} + \frac{T_D s}{1 + s \frac{T_D}{N}} \right) E(s)$$

Some rules of thumb

How does varying the parameters of a PID affect control performance?

Proportional action

$$U_P(s) = K_P E(s)$$

- a high value of K_P reduces the **steady-state error** and can make the system's response **faster**
- On the other hand, a too high value of K_P may **destabilize** the system

Proportional action

Steady-state error

- The residual steady state error can sometimes be handled with a **feedforward compensation** (e.g. resistive terms in electrical circuits)

$$\rightarrow U_P(s) = K_P E(s) + U_{FF}$$

Proportional action

Effect of noise

- Moreover, computing the tf from the measurement noise $n(t)$ to the output $y(t)$

$$Y(s) = \frac{K_p P(s)}{1 + K_p P(s)} (R(s) - N(s))$$

- A high K_p increases the system's bandwidth and **worsens the effect of measurement noise**

Integral action

$$U_I(s) = \frac{K_P}{T_I s} E(s)$$

- **null steady-state error** for constant $r(t)$ and $d(t)$
- **90° phase lag, bad for stability**
- may cause **actuator saturation**
(so-called integral *wind-up*)

Derivative action

$$U_D(s) = \frac{K_P T_D s}{1 + \frac{T_D}{N} s} E(s)$$

- 90° phase lead, **good for stability**
- amplifies the noise $n(t)$ at high-frequency, which may cause **actuator damage** for high control actions $u(t)$
→ choose N wisely!
- must be **cautious when dealing with discontinuous signals** (e.g. step reference)

Overview

- In general not all control actions need be present
 - P
 - I
 - PI
 - PD
 - PID

	stability	e_∞	T_a	overshoot
$K_P \uparrow$	Worsens	Decreases	Decreases	Increases
$T_I \downarrow$	Worsens	0 if $K_I \neq 0$	Decreases	Increases
$T_D \uparrow$	Improves	Not influenced	Not influenced	Decreases